Research of aerodynamics characteristics of wind power plant blades

M. Galdikas*, A. Vilkauskas**

*Kaunas University of Technology, Kęstučio 27, 44312 Kaunas, Lithuania, E-mail: mantas.galdikas@stud.ktu.lt
**Kaunas University of Technology, Kęstučio 27, 44312 Kaunas, Lithuania, E-mail: andrius.vilkauskas@ktu.lt

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1. Introduction

Nowadays a great deal of attention is paid to development and wide practical application of renewable energy sources. Wind energy is one of the most developed renewable energy spheres. Recently, vertical axis wind turbines because of their characteristics (low noise and bird friendly) are increasingly occupying a bigger part of the market in comparison to traditional horizontal axis wind turbines. Worldwide is known mostly popular horizontal axis power plants (HAWT), but lately vertical axis wind power plants (VAWT) are becoming more popular, because they have a lot of advantages such as low noise, more environmentally friendly and etc. [1]

This study examined the main types of wind power plants. Using flow designing fluid simulation software Solidworks Flow Simulation flow analysis of symmetrical and asymmetrical profile blades at different airflow velocities was performed. The analysis was carried out by changing the blade’s position in respect of the airflow in order to determine the optimum angles of attack. The results were analyzed to identify torques and angles of attack affecting the blades, which allowed deriving the maximum torque values. During designing process the graphs of operating torque were obtained according to an evaluation of blades’ rotation frequency. Angle of attack values power generated by rotor of analyzed blades were estimated. This analysis indicated that the asymmetrical blade generates a bigger torque and power than the same chord length blade of a symmetrical profile [2, 3].

2. Profiles of blades chose and analizing model designing

This work will analyze the blades of two profiles of different cross sections. The coefficients of coordinates of blade profiles are selected from the database of Illinois University Research Institute of Aircraft Engineering [4], which presents more than 1550 different profiles listed in the alphabetical order.

The profiles characteristic to wind power stations of vertical axis of Darrieus [5] type: symmetrical and asymmetrical (one flat side) aeroprofiles. It was decided to select the length of profile’s chord (that is the distance between the most remote points in profile’s cross section) as 200 mm, because this is the predominant length of chord in the power stations of smaller power.

The asymmetrical profile is selected as the blade profile AQUILA R/C created specially for laminar airflow. In order to receive the spacious model, which calculation results in the airflow were more real, the estimated length of the blade in 1000 mm is chosen. The designed Solidworks model is presented in Fig. 1.

Material of this blade is chosen carbon fibre – Hexcel AS4C. Area of cross-section 2485.84 mm², surface area excluded ends 405167.34 mm², model volume 2482538.53 mm³, weight 4,418 kg.

The symmetrical profile of blade is selected as EPPLER E297. The blade of this profile is also modeled at 1000 mm length so that the calculation results could be compared. The designed model in Solidworks environment is presented in Fig. 2.

Material of this blade is chosen carbon fibre – Hexcel AS4C. Area of cross-section 3055.43 mm², surface area excluded ends 404041.94 mm², model volume –
3053675.33 mm³, weight – 5.435 kg.

The models of these blades in Solidworks Flow Simulation program are put into the estimated area in the form of rectangular parallelepiped presented in Fig. 3, which dimensions are: 400×400×1000 mm. The length of the estimated area 1000 mm corresponds to the blade’s length, thus the modeled airflow does not get through the blade’s wings, and the calculation results should correspond the parameters of 1000 mm length blade in the real environment.

Fig. 3 Calculation area included blade

The Solidworks Flow Simulation program is used in this work to put the blades into 5 airflows of different speeds: 3, 8, 10, 12, 15 m/s. Such speeds of the airflows were selected because they are the most characteristic wind speeds – the speed from 3 to 8 m/s is such, at which the majority of wind power stations start working (rotating), while the speed from 12 to 15 m/s is the working (peak) speed of the wind, at which the wind power stations are working in maximal regime, i.e. the maximal power is acquired. The direction of airflow is considered stable in calculations – only the angle of blade’s attack is changed.

In case of each speed of the airflow the blades are rotated around their geometrical axis, which is derived through the geometrical centers of the profiles of blade cross sections, in 5 degrees of the entire circle – 360°. Therefore it is possible to observe the changing forces affecting the blade, torques, pressures, distribution of speeds of airflow as the blade’s position is changing with regard to the airflow.

In order to examine universally the aerodynamic characteristics of the blade, the results of the following calculations are expected: static, dynamic and summary flow pressure, projections of airflow’s speed to the axes x, y, z, and summary speed of flow, projections of normal forces affecting blade’s surface and affecting the entire blade to the axes x, y, z and summary force, projections of frictional forces of airflow affecting the blade’s surface to the axes x, y, z, and summary frictional force, and blade’s torque around axis z [6, 7].

3. Analysis of CAD results

3.1. Analysis of asymmetrical profile blade

After 360 calculations (rotation in 360° step by 5° in each position by airflows of 5 different speeds), the set values mentioned in chapter 1 are received. The further calculations of blade AQUILA R/C will use the values of forces affecting the blade, because the values of normal forces affecting the blade’s surface are very close to the values of forces affecting the blade, and their percentage expression is presented in (Eq. 1). Besides, the usage of forces affecting the blade in calculations simplifies them as they are concentrated in the blade’s axis:

\[
F = \left(1 - \frac{F_{45/12}^{sum}}{F_{45/12}^{sum}}\right) \times 100\%.
\]  

The force affecting the blade in the direction of z axis on average makes 0.001% of the summary force. Besides, this force does not create a torque around the rotation axis of the rotor; thus this force will not be taken into account in further calculations. Moreover, the frictional forces affecting the blade’s surface are smaller than 0.15 N, when the speed of airflow is maximal – 15 m/s, whereas the values of projections of the blade-affecting forces are significantly bigger, thus the frictional forces will not be taken into account in the further calculations, as well.

When all the forces of small values are rejected, it is received that the main torque of the wing around the rotor’s rotation axis is created by the projective components in the directions x and y of the force affecting the blade, together with the blade’s torque. The illustrative-estimated scheme of the forces and torques is presented in Fig. 4.

Fig. 4 Diagram of forces and moments operating blade: \(F_x, F_z\) – force’s projection to the x axis, \(N\); \(F_{45}, F_{12}\) – force’s projection to the y axis, \(N\); \(M_x, M_z\) – torque around the blade’s axis going through the geometrical centers of sections, Nm; \(a\) – variable angle of blade’s attack, degrees; \(L\) – arm of the torque created by blade around the axis of rotor’s center (O point in plane); \(v\) – speed of airflow, m/s

If the direction of the airflow is considered constant and only the angle of blade’s attack \(a\) is changed by step 5°, the Solidworks Flow Simulation program helps to receive results, which are systemized and illustrated graphically.
According to the diagram (Fig. 5), the values of force $F_x$ acquire both positive and negative values. Besides, the repetition of curves is noticed in case of each different speed of airflow. Therefore the conclusion can be made that the most effective angles of blade’s attack during formation of force $F_x$ are stable – regardless the speed of airflow. The maximal achievable force when the speed of airflow is 15 m/s – 21.5 N, when the blade’s turn to the airflow is 230°, and the smallest is equal to 20.7 N, when the blade’s turn to the airflow is 300°.

![Fig. 5](image)

**Fig. 5 Force $F_x$ dependence of angle on attack $\alpha$ (asymmetrical profile blade)**

According to the diagram (Fig. 6), the values of force $F_y$ are only positive. The same as in the case of force $F_x$, the repetition of curves is noticed in case of each different speed of airflow, thus the conclusion can be made that the most effective angles of blade’s attack during formation of force $F_y$ are stable – regardless the speed of airflow. The maximal achievable force when the speed of airflow is 15 m/s – 49.0 N, when the blade’s turn to the airflow is 265°, and the smallest is equal to 0.6 N, when the blade’s turn to the airflow is 180°.

![Fig. 6](image)

**Fig. 6 Force $F_y$ dependence of angle on attack $\alpha$ (asymmetrical profile blade)**

According to the diagram (Fig. 7), the values of force $F$ are only positive. The maximal achievable force when the speed of airflow is 15 m/s – 49.5 N, when the blade’s turn to the airflow is 280°, and the smallest is equal to 2.4 N, when the blade’s turn to the airflow is 175°.

![Fig. 7](image)

**Fig. 7 Force $F$ dependence of angle on attack $\alpha$ (asymmetrical profile blade)**

According to the diagram (Fig. 8), the values of torque $M$ are significantly positive, and negative ones are relatively small. The same as in the case of forces $F_x$ and $F_y$, the repetition of curves is noticed in case of each different speed of airflow, thus the conclusion can be made that the most effective angles of blade’s attack during formation of torque $M$ are stable – regardless the speed of airflow. The maximal achievable torque when the speed of airflow is 15 m/s – 4.9 Nm, when the blade’s turn to the airflow is 265°, and the smallest is equal to 0.5 Nm, when the blade’s turn to the airflow is 170°.

Following the scheme presented in Fig. 4 and received modeling results of the flows, the analysis is done, what the blade’s torque around the rotor’s rotation axis is when the blade travels in circle without changing its attack angle with regard to the rotor’s rotation axis. The estimated rotation diameter is selected to calculate the torques – 2 m. This means that the rotation radius of 1 m length (torque’s arm) will be used for calculations. Following the scheme presented in Fig. 4, the torque equation is written around the point O when the blade’s position is in the point 2:

$$M_{\phi_2} = -F_{x_2}L\sin\phi_2 + F_{y_2}L\cos\phi_2 + M_{c_2},$$

(2)

where $F_{x_2}$ is projection of blade-affecting force to the axis x, N; $F_{y_2}$ is projection of blade-affecting force to the axis y, N; $M_{c_2}$ is blade-affecting moment, Nm; L is beam of rotation of blade around point O, m; $\phi_2$ is rotation angle of blade, deg.

The calculations are done according to the received modeling results of the flows, thus the $\phi$ step is considered to be 5°. The cycle calculations of blade’s rotation around point O are done, according to the following system of equations:

$$M_{\phi_0} = -F_{x_0}L\sin\phi_0 + F_{y_0}L\cos\phi_0 + M_{c_0};$$

$$M_{\phi_0} = -F_{x_n}L\sin\phi_n + F_{y_n}L\cos\phi_n + M_{c_n};$$

$$M_{\phi_0} = -F_{x_3}L\sin\phi_3 + F_{y_3}L\cos\phi_3 + M_{c_3};$$

(3)

$M_{\phi_0} = -F_{x_3}L\sin\phi_3 + F_{y_3}L\cos\phi_3 + M_{c_3}$. 

$$M_{\phi_3} = -F_{x_3}L\sin\phi_3 + F_{y_3}L\cos\phi_3 + M_{c_3}.$$
According to the diagram (Fig. 9), the torque is quite unstable and pulsating as the blade’s position with regard to point O changes. Therefore the calculations of blade-affecting torques are done when the angle of blade’s attack $\alpha$ changes from $-175^\circ$ to $180^\circ$ by step $5^\circ$. The calculations are done analogically to the expressions presented in 2 and 3.

According to this sequence of blade-affecting torques (Fig. 10), the maximal and minimal values in each different point of $\phi$ depend on the angle of blade attack $\alpha$. Therefore in order to get the dependence of the angle of blade attack $\alpha$ from the blade’s rotation angle $\phi$ it is necessary to examine the sequence of torque curves presented in Fig. 10, by choosing maximal and minimal torques in each rotation angle $\phi$.

Maximal and minimal values shown in Fig. 11.

According to the received values, the bigger work performed by the torque is received when the curve is affected by the torques illustrated in $M_{\text{maximal}}$ torque curve. Following these calculations and dependence of blade-affecting torques on the attack angle $\alpha$ shown in Fig. 10, the dependence of the blade’s attack angle $\alpha$ is received in the blade’s position $\phi$ with regard to point O.

According to the diagram (Fig. 12), in the critical interval, which segment is from $175^\circ$ to $180^\circ$, the blade’s attack angle has to change by $185^\circ$ degrees.

### 3.2. Analysis of symmetrical profile blade

Due to EPPLER E297 profile is symmetrical, it is needed to perform only 180 calculations, after it was got 2.1 paragraph refered values. For the further EPPLER E297 blade calculations will be used forces and moments as assymetrical profile blade case.

When all the forces of small values are rejected, it is received that the main torque of the wing around the rotor’s rotation axis is created by the projective components in the directions x and y of the force affecting the blade, together with the blade’s torque. The illustrative-estimated scheme of the forces and torques is presented in Fig. 4.

If the direction of the airflow is considered constant and only the angle of blade’s attack $\alpha$ is changed by step $5^\circ$, analogy are got forces and torques dependences of angle on attack:

To determine, which working curve is more effective, it is necessary to determine, according to which curve the work performed by the torque is bigger. The value of work is received when the integral of the torque is calculated:

$$A_{M_{\text{min}}} = \int_0^{355} |M_{\text{min}}| d\phi;$$

$$A_{M_{\text{max}}} = \int_0^{355} |M_{\text{max}}| d\phi.$$
According to the diagram (Fig. 13), the values of force \( F_x \) acquire both positive and negative values. Besides, the repetition of curves is noticed in case of each different speed of airflow. Therefore the conclusion can be made that the most effective angles of blade’s attack during formation of force \( F_x \) are stable – regardless the speed of airflow. The maximal achievable force when the speed of airflow is 15 m/s – 17.3 N, when the blade’s turn to the airflow is 120° ir 240°, and the smallest is equal to 20 – 18.9 N, when the blade’s turn to the airflow is yra 55° ir 305°.

\[ \text{Fig. 14 Force } F_x \text{ dependence of angle on attack } \alpha \text{ (symetrical profile blade)} \]

According to the diagram (Fig. 14), the values of force \( F_y \) are only positive. The same as in the case of force \( F_x \), the repetition of curves is noticed in case of each different speed of airflow, thus the conclusion can be made that the most effective angles of blade’s attack during formation of force \( F_y \) are stable – regardless the speed of airflow. The maximal achievable force when the speed of airflow is 15 m/s – 50.5 N, when the blade’s turn to the airflow is 85° and 275°, and the smallest is equal to 0.04 N, when the blade’s turn to the airflow is 0° and 180°.

\[ \text{Fig. 15 Force } F_y \text{ dependence of angle on attack } \alpha \text{ (symetrical profile blade)} \]

According to the diagram (Fig. 15), the values of force \( F_z \) are significantly positive, and negative ones are relatively small. The same as in the case of forces \( F_x \) and \( F_y \), the repetition of curves is noticed in case of each different speed of airflow, thus the conclusion can be made that the most effective angles of blade’s attack during formation of torque \( M_z \) are stable – regardless the speed of airflow. The maximal achievable torque when the speed of airflow is 15 m/s – 5.1 Nm, when the blade’s turn to the airflow is 85° and 275°, and the smallest is equal to -0.08 Nm, when the blade’s turn to the airflow is 25° and 335°.

\[ \text{Fig. 16 Moment } M_z \text{ dependence of angle on attack } \alpha \text{ (symetrical profile blade)} \]

According to the diagram (Fig. 16), the values of torque \( M_z \), are significantly positive, and negative ones are relatively small. The same as in the case of forces \( F_x \) and \( F_y \), the repetition of curves is noticed in case of each different speed of airflow, thus the conclusion can be made that the most effective angles of blade’s attack during formation of torque \( M_z \) are stable – regardless the speed of airflow. The maximal achievable torque when the speed of airflow is 15 m/s – 5.1 Nm, when the blade’s turn to the airflow is 85° and 275°, and the smallest is equal to -0.08 Nm, when the blade’s turn to the airflow is 25° and 335°.

\[ \text{Fig. 17 Moment of blade dependence on blade position according to point O (symetrical profile blade)} \]

According to the diagram (Fig. 17), the torque is quite unstable and pulsating as the blade’s position with regard to point O changes. Therefore the calculations of blade-affecting torques are done when the angle of blade’s attack \( \alpha \) changes from -175° to 180° by step 5°. The calculations are done analogically to the expressions presented in Eqs. (2) and (3).

\[ \text{Fig. 18 Moment of blade dependence on blade position according to point O, when angle of attack } \alpha \text{ is variable (symetrical profile blade)} \]

According to the diagram (Fig. 18), it is found more effective curve and ascertained blade’s attack angle \( \alpha \) depending on blade’s position \( \varphi \) with regard to point O.

In this case there is different regularity than...
Assymetrical blade. Maximal torques according point O are achieved when there are two different angles of blade attack. Therefore there is eliminating curve which means higher fluctuation of angle of attack. After eliminating it is got new curve.

According to the dependence (Fig. 21), in the critical interval, which segment is from 185° to 190°, the blade’s attack angle has to change by 170° degrees.

The pulsation of torque of rotor with three blades is significantly smaller even when it is compared to the pulsation of torque of rotor with two blades.

4. Moments calculation of rotors made from few blades

Until now it has been analyzed, what torques appear when one blade is in the airflow. Below the summary torques are calculated when the wind-wheel (rotor) consists of two or three blades. The bigger number of blades is not taken into account because the modeling peculiarities of airflow may result in additional errors, which appear when the overlap of blades is not taken into account, due to increased turbulences of flows, etc.

First of all, the diagrams of torques of the blade of asymmetrical profile AQUILA R/C profile are received for comparison with one blade and when two (180° with regard to each other) and three (120° with regard to each other) blades are combined. The summary torques are encountered when the torques of each point are summed up by moving them by certain number of degrees.

According to the Fig. 22, in presence of different number of blades, not only the torque generated by the rotor but also the pulsation of torques differ. The pulsation of torques is calculated in percentage expression of relation of difference between the maximal and minimal torques with maximal torque:

\[
P_1 = \left( \frac{M_{1\text{max}} - M_{1\text{min}}}{M_{1\text{max}}} \right) \times 100\% ;
\]

\[
P_2 = \left( \frac{M_{2\text{max}} - M_{2\text{min}}}{M_{2\text{max}}} \right) \times 100\% ;
\]

\[
P_3 = \left( \frac{M_{3\text{max}} - M_{3\text{min}}}{M_{3\text{max}}} \right) \times 100\% .
\]

The analogous calculations of torques with different numbers of blades are done for the rotor with blades of the symmetrical profile EPPLER E297 with one blade and when two (180° with regard to each other) and three (120° with regard to each other) blades are combined. The summary torques are encountered when the torques of each point are summed up by moving them by certain number of degrees.

\[
P = \frac{A}{t},
\]

where: \( t \) is time of one period, \( s \); \( A \) is job of rotary moment, \( J \); calculated integrating rotary moment:

\[
A = \int_{0}^{355} |M| d\phi ,
\]

where: \( M \) is rotary moment of rotor, \( \text{Nm} \); \( \phi \) is turn of blade, rad.

When the obtained values are used, the nominal power generated by the rotor of asymmetrical profile (when the rotor does not rotate and the wind’s speed is 15 m/s) is received:

\[P_1 = 138.25 \, \text{W}, \text{ when the rotor consists of 1 blade};\]
\[P_2 = 276.50 \, \text{W}, \text{ when the rotor consists of 2 blades};\]
\[P_3 = 414.75 \, \text{W}, \text{ when the rotor consists of 3 blades}.\]

The analogous calculations of torques with different numbers of blades are done for the rotor with blades of the symmetrical profile EPPLER E297 with one blade and when two (180° with regard to each other) and three (120° with regard to each other) blades are combined. The summary torques are encountered when the torques of each point are summed up by moving them by certain number of degrees.
Fig. 23 Moments of rotor composited from different amount of blades

The torque pulsations are calculated analogically:

\[
\begin{align*}
 p_1 &= \frac{M_{1\text{max}} - M_{1\text{min}}}{M_{1\text{max}}} \times 100\% ; \\
p_2 &= \frac{M_{2\text{max}} - M_{2\text{min}}}{M_{2\text{max}}} \times 100\% ; \\
p_3 &= \frac{M_{3\text{max}} - M_{3\text{min}}}{M_{3\text{max}}} \times 100\% .
\end{align*}
\]

(11)

(12)

(13)

Analogically to the blade of asymmetrical profile, it is seen that the pulsation of torque of rotor with three blades is significantly smaller even when it is compared to the pulsation of torque of rotor with two blades

When the obtained values are used, the nominal power generated by the rotor of asymmetrical profile (when the rotor does not rotate and the wind’s speed is 15 m/s) is received:

\[
\begin{align*}
P_1 &= 126.24 \text{ W}, \text{ when the rotor consists of 1 blade;} \\
P_2 &= 252.48 \text{ W}, \text{ when the rotor consists of 2 blade;} \\
P_3 &= 378.72 \text{ W}, \text{ when the rotor consists of 3 blade.}
\end{align*}
\]

Besides, it is noticed that the torque and generated nominal power of the rotor with the blades of symmetrical profile are smaller, and the pulsation of torque is bigger. And these are negative factors with regard to effectiveness and durability of construction, i.e. bigger pulsation causes bigger vibrations of the rotor.

5. Conclusions

1. The testing results of flows of blades of two different profiles helped to determine the following:
   - the blade-affecting forces and torques depend on their position with regard to the rotation axis;
   - the blade-affecting torques depend on the attack angles of blades. The optimal blade attack angles were encountered, in presence of which the biggest torques are generated. The dependences of attack angles on the position of blades around the rotation axis were formed. The critical change angles of blade attack were determined;
   - the work curves of torques generated by blades were modeled taking into account the speed of resistance airflow, which appears when the blade moves in orbicular trajectory.

2. There were determined the values of torques generated from the analyzed blades, which form the rotors. The pulsation of maximal torque was calculated in presence of different numbers of blades. It was determined that when rotor consists of three blades, the pulsation is the smallest and its values are equal to 4.41%, when the blade’s profile is asymmetrical, and to 6.05%, when the blade’s profile is symmetrical. As the power created by the torque generated by the blade of symmetrical profile is smaller and pulsation is bigger if compared to the asymmetrical profile, it is considered that the blades of asymmetrical profile are more suitable for the wind power stations of Darrieus type.

References


momentą, tuo pačiu ir galią, negu simetrinio profilio men- tė.

M. Galdikas, A. Vilkauskas

RESEARCH OF AERODYNAMICS
CHARACTERISTICS OF WIND POWER PLANT
BLADES

S u m m a r y

The article presents using flow designing fluid simulation software SolidWorks Flow Simulation flow analysis of symmetrical and asymmetrical profile blades at different airflow velocities was performed. The analysis was carried out by changing the blade’s position in respect of the airflow in order to determine the optimum angles of attack. The results were analyzed to identify torques and angles of attack affecting the blades, which allowed deriving the maximum torque values.

During designing process the graphs of operating torque were obtained according to an evaluation of blades’ rotation frequency. Angle of attack values under braking conditions and power generated by rotor of analyzed blades were estimated. This analysis indicated that the asymmetrical blade generates a bigger torque and power than the same chord length blade of a symmetrical profile.

Keywords: wind power plant, blade, flow, angle of attack (pitching).

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